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for a Professional Development Guide and Argumentation Lesson Planning Template, as well as posters, handouts, digital mathematics tools, and other resources.